

Applications of Linear and Nonlinear Properties of Crystalline Whispering Gallery Mode Resonators

Lute Maleki OEwaves, Inc. and JPL Pasadena, CA Lute.Maleki@oewaves.com



Contributors

- Vladimir Ilchenko
- Anatoliy Savchenkov
- Andrey Matsko
- Makan Mohageg
- Ivan Grudinin
- David Seidel
- Wei Liang



- Introduction
- Fundamentals of crystalline WGM resonators
- Spectrum engineering
- Delay-slow light devices
- Filters
- Modulators and receivers
- Novel sources based on nonlinearities
- Conclusions



• Introduction

- Fundamentals of crystalline WGM resonators
- Spectrum engineering
- Filters
- Modulators and receivers
- Novel sources based on nonlinearities
- Conclusions



What are WGM resonators

- Whispering Gallery Modes are electromagnetic resonances that occur in circularly symmetric dielectrics, and trap light in a circling orbit via total internal reflection
- They can be produced in a variety of shapes
- They can be produced in a variety of sizes (10's of mm to μ m)
- They can be fabricated from a variety of materials
- They can be made with various fabrication processes



Features of WGM Resonators

- Ultra-high Q allows long optical delays (ns to ms range)
- Ultra-narrow spectral linewidth makes them ideal filters
 - Photonic microwave filters with microwave signals carried as sidebands on an optical carrier --- any microwave frequency can be supported
 - Multi-resonator structures with high rejection band (~ 100 dB)
 - Optical filters for signal processing, spectroscopy, laser stabilization, ...
- Resonators made using materials with electooptic effect can lead to
 - Tunable filters (optical and microwave) with > 40 GHz tunablity
 - Highly efficient modulators
 - Optical memory using photorefractivity



Applications

- Linear regime
 - Cavity QED
 - "Artificial" atoms and molecules
 - Spectroscopy and materials studies
 - Filters (fixed and tunable; microwave and optical)
 - Modulators
 - Delays
 - Slow light (multi-resonator structures)
- Nonlinear regime
 - Lasers (including Raman lasers) and THz sources
 - OPO



• Introduction

- Fundamentals of crystalline WGM resonators
- Spectrum engineering
- Filters
- Modulators and receivers
- Novel sources based on nonlinearities
- Conclusions



Whispering Gallery Modes for Spherical Resonators

$$\nabla \times (\nabla \times E) + \frac{\varepsilon}{c^2} \frac{\partial^2 E}{\partial t^2} = 0$$

$$(\nabla^{2} + k^{2}) \cdot \vec{e} = 0$$

$$e = \sum_{l,m} [R_{TE}(r)Y_{l}^{m}(\theta, \phi) + \frac{1}{\varepsilon} \nabla \times (R_{TM}(r)Y_{l}^{m}(\theta, \phi))]$$

$$\frac{\partial^{2}R}{\partial r^{2}} + [k^{2}\varepsilon - \frac{l(l+1)}{r^{2}}]R = 0$$
interval
Num
$$R_{TM}(r)Y_{l}^{m}(\theta, \phi) = 0$$

Whispering Gallery Modes are
electromagnetic resonances which occur in circularly
symmetric dielectrics. These resonators trap light
in a circling orbit via total
internal reflection .The WGM usually is characterized by mode
Numbers n, l, and m (ϕ))is the radial mode number
is the angular mode number

m is the azimuthal mode number

 $J_{l+1/2}(kr)$ is the solution

$$k_{l,q} = \frac{1}{a\varepsilon_0} \left[l + \alpha_q \left(\frac{l}{2}\right)^{1/3} - \sqrt{\frac{\varepsilon_0}{\varepsilon_0 - 1}} + \frac{3\alpha_q^2}{20} \left(\frac{2}{l}\right)^{1/3} + \dots \right]$$

$$H_{\rho} = n(n+1)\frac{\sqrt{k_{p}\rho}}{\rho^{2}}J_{n+\frac{1}{2}}(k_{p}\rho)P_{n}^{m}(\cos\theta)\sin(m\phi)$$





Crystalline WGM resonator

- Extremely high Q (> 10¹¹ has been demonstrated at JPL, finesse>10⁷)
 - Long delays (micro seconds)
 - Narrow optical/phtonic filters
 - Reference resonator for laser stabilization
- Small mode volumes for exploring nonlinear effects
 - Second harmonic generation with great efficiency
 - Efficient parametric processes (four-wave mixing, up/down conversion)
 - Entangled photon source
- Crystalline material with electooptic effects
 - Frequency tunability
 - Highly efficient modulators
 - Optical memory using photorefractivity
- Support wide wavelength range (from THz to UV)
 - Unique feature, very different from FP cavity
- Small sizes: ranging from 10's of micron to a few mm
 - Compact
 - Easier for mechanical and thermal stabilization



Types of Whispering Gallery Mode Resonators



Calcium fluoride resonators that have $Q=2 \times 10^{10}$. Crystalline disk Q~3ex10¹¹ L. Maleki et al, Physical Review A 70, 051804(R) 2004.



Fused silica microtoroid q \sim 1 x 10⁸ K. Vahala et al., Nature, vol 421, 27 February 2003 p. 925.



Silicon microdisk, Q~5 x 10⁵ O.Painter et al. App. Phys.Let. Vol 85 No 17, 25 October 2004



Toroidal resonator fabricated by placing a melting sphere between two fibers



Micro-ring resonators. $Q \sim 10^4$ to 10^7 . $R \le 100 \ \mu m$



Solid H2, Q>10⁹ K.Hakuta et al. Opt.Lett.,27 No 6 March 15 2002



silica microsphere Q=8x10⁹

New crystalline ultra-high Q microcavities







Non-spherical Structures





Toroidal Resonators



Disk Resonators



Elliptical Resonators









Coupling with Low Insertion Loss



With prism coupling and elliptical resonator



Optical Loss Mechanisms

- Linear Loss
 - Radiative : $\alpha_{radiative} = Ae^{-l}$
 - Intrinsic material loss: $Q_{material} = \frac{2\pi l}{\alpha_{material}\lambda}$
 - Surface loss: $Q_{surface} = \frac{\lambda^2 R}{\pi \sigma^2 B}$, σ and B are surface inhmogeneity parameters.

$$Q^{-1} = Q_{rad}^{-1} + Q_{surface}^{-1} + Q_{material}^{-1}$$

- Nonlinear Loss
 - SRS, FWM, Parametric processes





E.D.Palik, "Handbook on optical constants of solids", Academic, NY, 1998







The ring-down measurement of a fluorite WGM resonator life time





Time, µs















	775nm	1064nm	1319nm	1550nm
α -Al ₂ O ₃	8x10 ⁷		1.5x10 ⁹	
Quartz				5x10 ⁹
SLN	7x10 ⁷	8x10 ⁷	2x10 ⁸	6x10 ⁸
SLT	7x10 ⁷		2x10 ⁸	2x10 ⁹
Fused Silica	8x10 ⁹			
MgF ₂			>10 ¹⁰	
CaF ₂	>6x10 ¹⁰	>6x10 ¹⁰	>4x10 ¹⁰	3x10 ¹¹





- Introduction
- Fundamentals of crystalline WGM resonators
- Spectrum engineering
- Filters
- Modulators and receivers
- Novel sources based on nonlinearities
- Conclusions



Frequency spectrum and mode volume can be engineered by design of the resonator profile







Single mode WGM resonators





More on single mode WGM resonators: true single mode spectrum





White light WGM resonators





Novel configuration of whispering gallery mode resonators



STM picture of a single mode resonator being a "rim" over a multimode wave guide $\varepsilon = \varepsilon_0 \left(1 + \frac{2L(z)}{R_0} \right)$



(a) After

 diamond
 turning
 (b) After proper
 tune-up





Delay line with coupled resonators



Field distribution



- Introduction
- Fundamentals of crystalline WGM resonators
- Spectrum engineering
- Slow light devices
- Filters
- Modulators and receivers
- Novel sources based on nonlinearities
- Conclusions



Coupled resonator systems



- "Slow light" and SCISSOR solitons J. Heebner and R. Boyd, JOSA B 19, 722 (2002) and J. Mod.Opt. 49, 2629 (2002).
- Coupled cavities for enhancing cross-phase modulation in EIT

T. Opatrny and D. Welch, Phys. Rev. A 64, 023805 (2001)

 Sharp asymmetric line shapes in side coupled waveguide-cavity systems

S. Fan, Appl. Phys. Lett. 80, 908 (2002).

• Storing light all optically

M. Yanik and S. Fan, quant-ph/0312027 (2003).



An analogy with EIT in quantum systems: interference of decays







- Introduction
- Fundamentals of crystalline WGM resonators
- Spectrum engineering
- Filters
- Modulators and receivers
- Novel sources based on nonlinearities
- Conclusions



WGM Filters

- WGM filters are a powerful new tool for photonic processing of RF signals and enable new capabilities
- WGM tunable filters offer wide tunability range with submicrosecond tuning speed
- OEwaves has demonstrated single and multi-pole filters with tunability exceeding 12 GHz; fast tuning speed has been demonstrated with measurement of waveform


Photonic filters





Lithium Niobate Whispering Gallery Mode Resonators in optical frequency domain



Photograph of 1 mm size WGM resonator disk Optical coupling scheme for the disk resonator

Features:

- Large quality factor
- Large electro-optical tuning range: 20 GHz per 150 V
- Insertion loss: 2-7 dB
- Small size: 0.1-12 mm

• $Q = 8 \times 10^8$ at $\lambda = 1550$ nm $Q = 2 \times 10^8$ at $\lambda = 1310$ nm $Q = 8 \times 10^7$ at $\lambda = 1064$ nm $Q = 7 \times 10^7$ at $\lambda = 780$ nm



Tri-pole tunable filter prototype

Characteristic third order filter function and 12 GHz tuning











Single mode "Vernier"



Tri-Pole Filter Architecture of AOSP Phase II







Orthogonal Flexture-based Mechanical Design of Six-pole Optical Filter (AOSP)



- Independent mech. trimming of all couplings
- Improved linearity and stability
- Tap coupler/PD at third resonator for alignment



Outline

- Introduction
- Fundamentals of crystalline WGM resonators
- Spectrum engineering
- Filters
- Modulators and receivers
- Novel sources based on nonlinearities
- Conclusions



WGM based EOM

The carrier and sidebands have the same polarization





First High Performance WGM Modulator Fabricated With Lithium Niobate

V. S. Ilchenko, A. A. Savchenkov, A. B. Matsko, and L. Maleki, JOSA B, 20, 333 (2003).

Generates mostly phase modulated light so the RF return is relatively low.



Input power, dBm



Characteristics of WGMR Modulators

- Narrow Bandwidth (< 20) MHz
- Low RF Saturation power
- Low optical power handling capability

Ideal for applications such as in oscillators (OEO) and narrowband receivers--- BUT Limited for other applications



WGMR Modulator as a Receiver



First High Performance WGM Modulator Fabricated With Lithium Niobate

V. S. Ilchenko, A. A. Savchenkov, A. B. Matsko and L. Maleki, JOSA B, 20, 333 (2003).

Highly Effective Modulation Using Electro-Optic Effect



Empty Base



SSB Modulator



Typical suppression of the sidemode is $\sim 30 \text{ dB}$



WGM SSB versus conventional WGM EOM











SSR measurements

Second sideband level determines crosstalk between frequency channels





Maximum RF return = +9dBm It exactly corresponds to SSB equation: $P_{RF}=P_{carrier}+P_{sideband}+G$, where $P_{carrier}=+13dBm$, $P_{sideband}=+13dBm$ G=-17.4dB

$$G = 1 \ 1 \ \frac{R^2 \rho}{2}; Rg 0.8, \rho = 55, G = -0 \ .4d$$

SSB Tunability



- Wide tunability from -90 to +90V (2-18GHz)
- Linear tuning
- Efficiency dips < 2dB





SSB Modulator Characteristics

- Higher RF saturation (but still lower than 10 mW)
- Larger bandwidth (100 MHz to 1 GHz possible)
- Very large RF return (nearly optimal power in sideband)
- Center frequency widely tunable (1-40 GHz possible)

A new class of optical modulator







Hyper-parametric oscillations based on FWM in a fluorite resonator





Outline

- Introduction
- Fundamentals of crystalline WGM resonators
- Spectrum engineering
- Filters
- Modulators and receivers
- Novel sources based on nonlinearities
- Conclusions

Efficiency of the frequency conversion with a WGM PPLN resonator and spectra of the pump and signal



V. S. Ilchenko et al., Phys. Rev. Lett. 92 (4): art. no. 043903 (2004)



Hyperparametric Oscillation

The reverse of the frequency doubling is parametric generation of photon pairs (sub-threshold) or of squeezed vacuum (above-threshold).

The OPO threshold in our case is

$$P_{th} = \frac{\varepsilon_p \varepsilon_s^2}{(8\pi)^3 (\chi^{(2)})^2} \left(\frac{V_s}{V_{pss}}\right)^2 \frac{\omega_p V_p}{Q_s^2 Q_p}$$

Which can be as low as 1.5 pW. (The state of the art is 0.5 mW)



Hyper-parametric oscillations in fluorite resonators







Second-order ($2\Omega_{FSR}$) beat note is insignificant

> Raman scattering is not observed (expected at 322 cm⁻¹)

A.A.Savchenkov et al., Submitted to PRL (2004)



Phase noise of oscillations





Analysis

Kerr Hamiltonian: $H = H_0 + V$, $H_0 = \hbar \omega_0 a^{\dagger} a + \hbar \omega_+ b_+^{\dagger} b_+ + \hbar \omega_- b_-^{\dagger} b_-$, where

$$V = -\hbar \frac{g}{2} \left(a^{\dagger} a^{\dagger} a a + b^{\dagger}_{+} b^{\dagger}_{+} b_{+} b_{+} + b^{\dagger}_{-} b^{\dagger}_{-} b_{-} b_{-} \right) - 2\hbar g \left(b^{\dagger}_{-} b^{\dagger}_{+} b_{+} b_{-} + a^{\dagger} b^{\dagger}_{+} b_{+} a + a^{\dagger} b^{\dagger}_{-} b_{-} a \right)$$

Self-phase modulation

 $-\hbar g \left(b_{-}^{\dagger} b_{+}^{\dagger} a a + a^{\dagger} a^{\dagger} b_{+} b_{-} \right)$

Cross-phase modulation

Four-wave mixing

Equations of motion in an open system:

$$\begin{split} \dot{a} &= -(i\omega_{0} + i\kappa(T) + \gamma_{0} + \gamma_{c0})a + ig[a^{\dagger}a + 2b_{+}^{\dagger}b_{+} + 2b_{-}^{\dagger}b_{-}]a + 2iga^{\dagger}b_{+}b_{-} + f_{0} + f_{c0}, \\ \dot{b}_{+} &= -(i\omega_{+} + i\kappa(T) + \gamma_{+} + \gamma_{c+})b_{+} + ig[2a^{\dagger}a + b_{+}^{\dagger}b_{+} + 2b_{-}^{\dagger}b_{-}]b_{+} + igb_{-}^{\dagger}aa + f_{+} + f_{c+} \\ \dot{b}_{-} &= -(i\omega_{-} + i\kappa(T) + \gamma_{-} + \gamma_{c-})b_{-} + ig[2a^{\dagger}a + 2b_{+}^{\dagger}b_{+} + b_{-}^{\dagger}b_{-}]b_{-} + igb_{+}^{\dagger}aa + f_{-} + f_{c-} \\ \swarrow \\ \uparrow \\ \text{Temperature} \\ \text{tuning} \\ \text{Where} \quad \langle f_{c0} \rangle = \sqrt{\frac{2\gamma_{c0}P_{0}}{\hbar\omega_{0}}} e^{-i\omega t} \text{ and } g = \omega_{0}\frac{n_{2}}{n_{0}}\frac{\hbar\omega_{0}c}{\mathcal{V}n_{0}} \end{split}$$

Optical comb and 25 GHz RF generation

OEwaves



A. A. Savchenkov et al., "Tunable Optical Frequency Comb with a Crystalline Whispering Gallery Mode Resonator," Phys. Rev. Lett. 101, 093902 (2008).



Optical comb at 13.8 GHz



I. S. Grudinin, N. Yu, and L. Maleki, Opt. Lett. 34, 878-880 (2009)



Stimulated Raman Scattering & nonlinear decay



The scheme of the experimental setup. (A) The frequency of a continuous wave Nd:YAG laser was slowly swept across the free spectral range of the resonator. When coupling of the light to a whispering gallery mode exceeded 30 % the light was abruptly switched off with an electrooptic modulator triggered by an oscilloscope. In this configuration critical coupling (all light is entering the resonator) corresponds to zero signal on the photodiode, while zero coupling corresponds to the maximum signal on the photodiode. (B) The light exiting the resonator was collimated and geometrically separated from the Stokes light.





Typical ringdown characteristics of the fluorite WGM resonator. The solid line corresponds to the experimental observation, and the dotted line – to the theoretical simulation.

The spectrum of light exiting the Raman-active WGM resonator. The inset shows the structure of the Stokes line. The wavelength difference between the peaks shown in the inset corresponds to the free spectral range of the resonator.

A. A. Savchenkov, et al Opt. Lett. 32, 497-499 (2007).



Ultra-low threshold multi-order SRS



I. S. Grudinin and L. Maleki, Opt. Lett. 32, 166-168 (2007)



A)SRS threshold for a 1 mm ideal-surface cavity made with an ideal CaF_2 .

B) Low temperature SRS threshold for a 1 mm ideal cavity made with CaF_2 in terms of photon number.

C) Theoretically evaluated wavelength dependence of the Raman gain in CaF_2 .

I. Grudinin, A. B. Matsko, and L. Maleki, Opt. Express 15, 3390 (2007).


Stimulated Brillouin Scattering



Pump and SBS lines for fluorite cavity. The pump power was 50μ W. The two Stokes lines have frequencies red-shifted by 17.7 GHz (weak backward Stokes is seen because of the residual Rayleigh scattering) and by ~35 GHz (strong Stokes line created by the backward Stokes). The width of each line is limited by the OSA resolution of 0.012 nm.

I. S. Grudinin et al., Phys. Rev. Lett. 102, 043902 (2009).





 v_1 and v_2 are resonant with cavity WG modes, v_3 corresponds to 17.7GHz phonons.





Summary





Low thresholds of nonlinear effects

Very high Q-factor and small volume significantly reduce the threshold for various nonlinear optical processes in crystalline WGM disk resonators using low power CW laser excitation. This helps the study of nonlinear phenomena in crystalline material and results in development of novel optical and microwave photonic devices.

